MathFinance 346/Stat 391. Winter 2005. Homework 3. Due Wed 1/26.

All exercises use the notation in Schweizer's (1992) paper. Except in problem 5, you can assume that the short rate r = 0.

1. If the risk neutral measure coincides with the "minimal martingale measure"  $\hat{P}$ , find the market price of risk in the following *P*-Brownian motions:  $B_t$ ,  $\epsilon_t$ ,  $\xi_t$ , and  $N_t$ .

2. Find the sensitivity of the hedging strategy to the initial value:  $\partial \theta_t^* / \partial L$ . (Give as explicit an expression as you can).

3. Assume that all the coefficients  $(\mu, \sigma, m, v \text{ and } \rho)$  are nonrandom and constant. Find, as explicitly as you can, the hedging strategy for a European call on  $S_T$  with strike K.

4. Assume that all the coefficients  $(\mu, \sigma, m, v \text{ and } \rho)$  are nonrandom and constant. Find, as explicitly as you can, the value L that minimizes

$$\min_{\theta \in \Theta} E(\Pi + L - G_T(\theta))^2.$$

Give L for the European call on  $S_T$  with strike K.

5. Assume that the short term interest rate is non-zero. Show how to adapt Schewizer's results to this case. Discuss what conditions need to be imposed on the interest rate.