Modeling & Analyzing Massive Terrain Data Sets (STREAM Project)

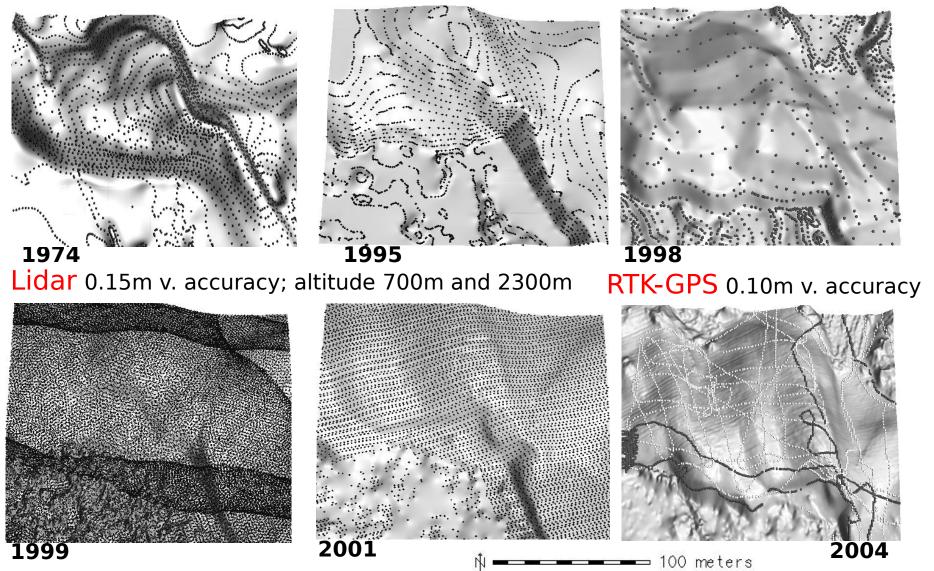
Pankaj K. Agarwal



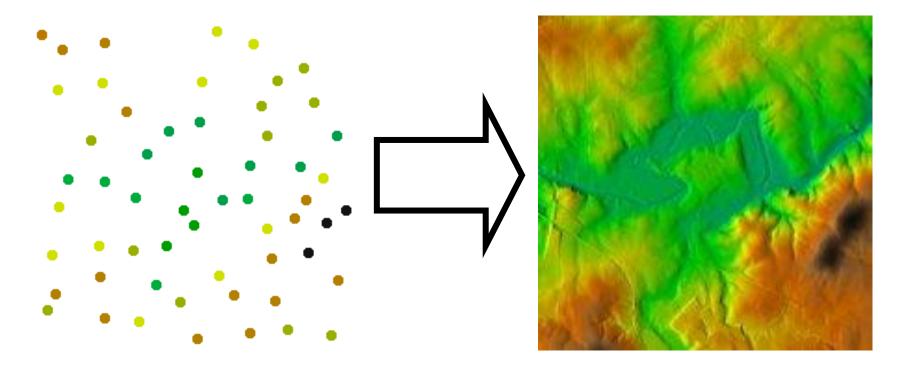
Workshop on Algorithms for Modern Massive Data Sets

Diverse elevation point data: density, distribution, accuracy

Photogrammetry 0.76m v. accuracy (5ft contours)



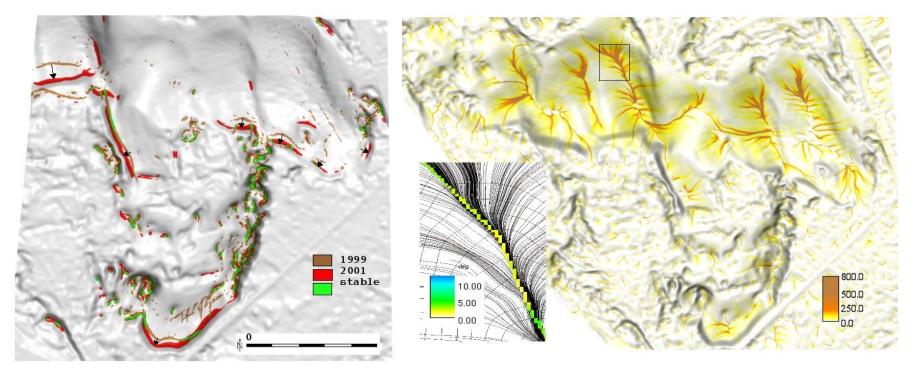
Constructing Digital Elevation Models



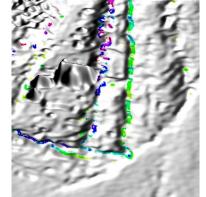
Grid DEM: Elevation stored at uniform grid points TIN: Triangulation; elevation stored at vertices Contours Maps: Iso-contour lines at regular intervals

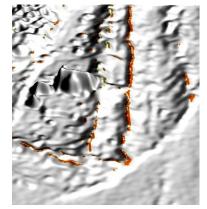
Natural feature extraction

Maps of topo parameters: computed simultaneously with interpolation using partial derivatives of the RST function, terrain features: combined thresholds of topo parameters



Extracted foredunes 1999-2004 using profile curvature and elevation threshold





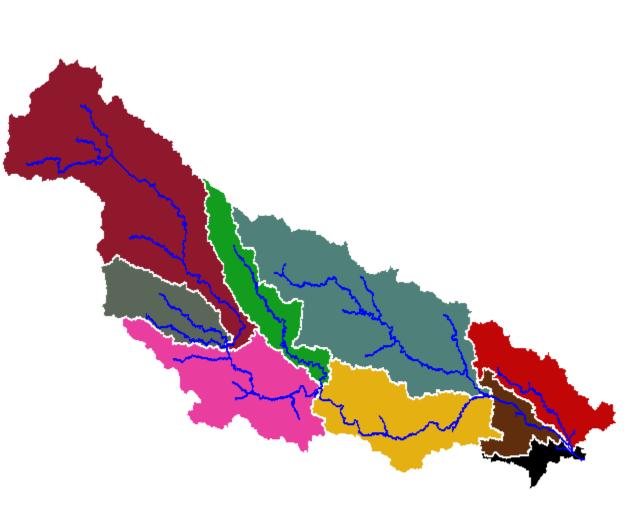
Tracking Evolving Features

slip faces: slope > 30deg 1995 new slip face in 1999 2001 25.00 20.00 15.00 10.00 dune crests: profile curvature threshold 0.010000 convex 0.000000 1974 1995 1998 concave -0.010000

how to automatically track features that change some of their properties over time?

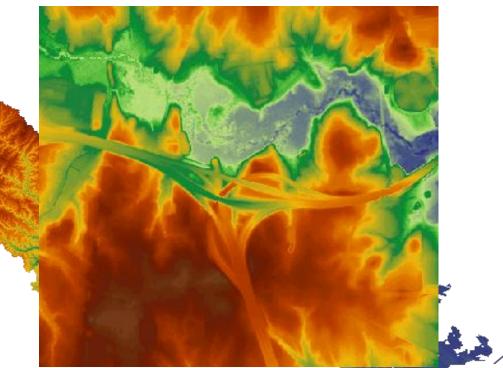
Terrain Analysis

- Flow Analysis
- Watershed
 hierarchy
- Visibility
- Navigation



Challenge: Massive Data Sets

- LIDAR
 - NC Coastline: 200 million points over 7 GB
 - Neuse River basin (NC): 500 million points over 17 GB
 - Applachian Range: 50GB-5TB
- Output is also large
 - 10ft grid: 10GB
 - 5ft grid: 40GB 💐



Approximation Algorithms

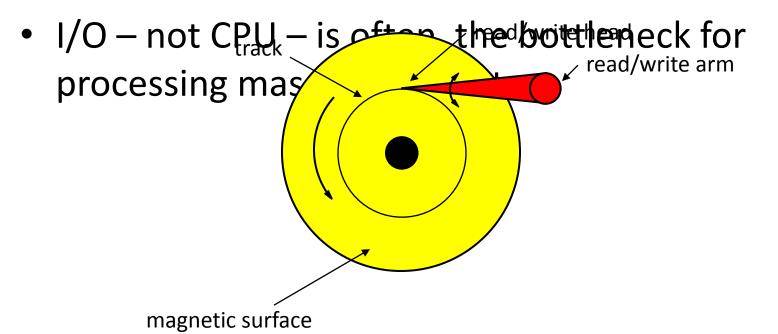
• Exact computation expensive

Many practical problems are intractable Multiple & often conflicting optimization criteria Suffices to find a near-optimal solution

- Tunable Approximation algorithms
 - Tradeoff between accuracy and efficiency
 - User specifies tolerance

I/O-Bottleneck

- Data resides in secondary memory
- Disk access is 10⁶ times slower than main memory access
 - Maximize useful data transferred with each access
 - Amortize large access time by transferring large contiguous blocks of data



I/O-efficient Algorithms [AV88]

Disk

B

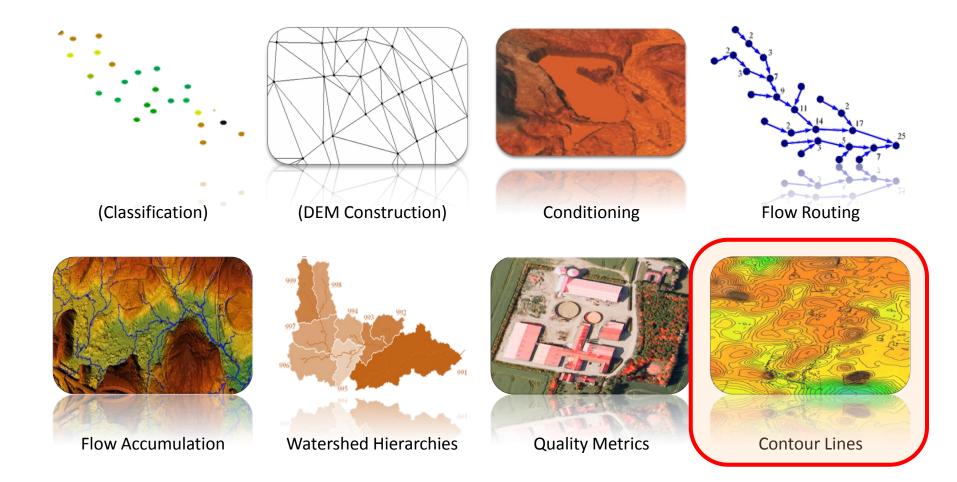
RAM

- Traditional algorithms optimize CPU computation
 - Not sensitive to penalty of disk access
- I/O model
 - Memory is finite
 - Data is transferred in blocks (B: block size)
 - Complexity: #disk blocks transferred (#I/Os)

Scan(N) = O(N/B)Sort(N) = $O(\frac{N}{B} \log_{\frac{M}{B}} \frac{N}{B})$ B ~ 2K-8K

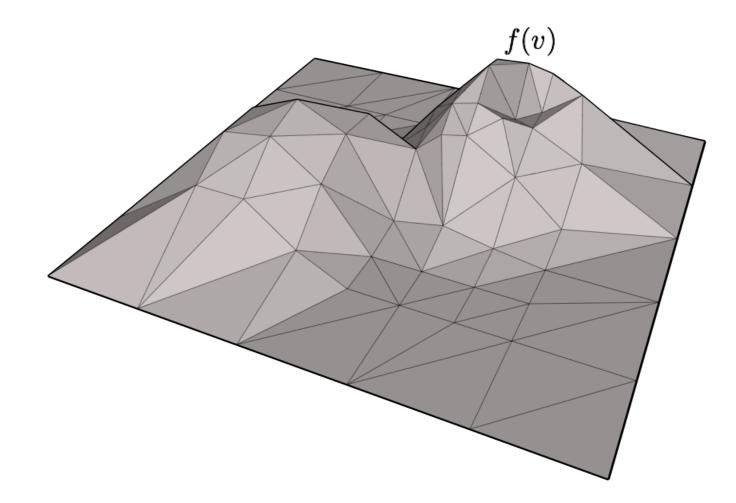
External Memory Algorithms [Vitter]

The TerraStream Modules



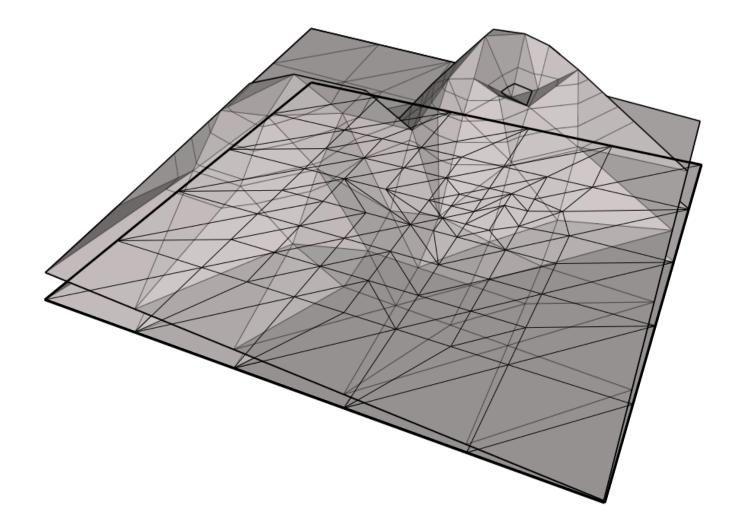
TIN DEM

Given a plane triangulation Σ with with a height f(v) for each vertex v, one can linearly interpolate f in the interior of every face of Σ .



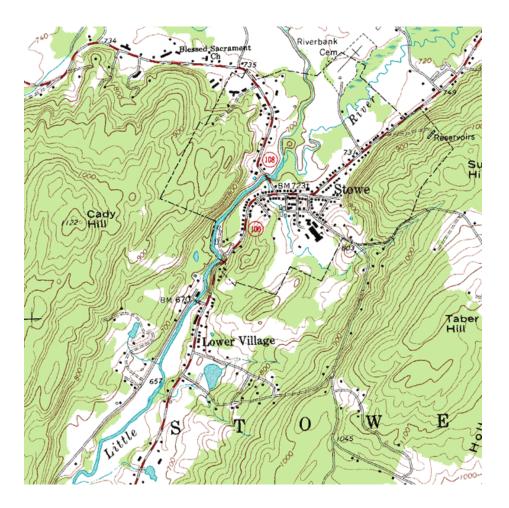
Level Sets, Contours

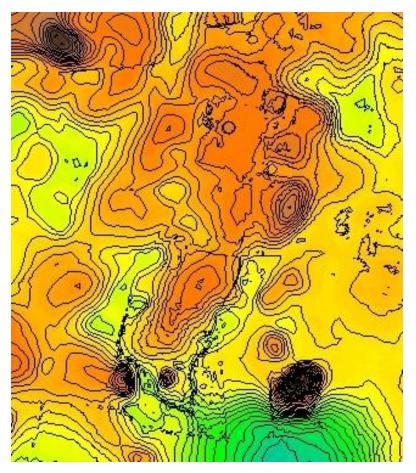
The level-set at height l is $f^{-1}(l)$. Each connected component of a level set is called a contour. Given levels $L = \{l_1, \ldots, l_k\}$, the contour map is $f^{-1}(L)$.



Contour Maps

Given a set of levels $L = \{l_1, \ldots, l_k\}$, compute the contour map $f^{-1}(L)$ such that each contour is reported separately and in sorted (circular) order.





Contour Maps

 Usage of contour lines (also called iso-contours, isogons, etc) goes back to at least 17th century

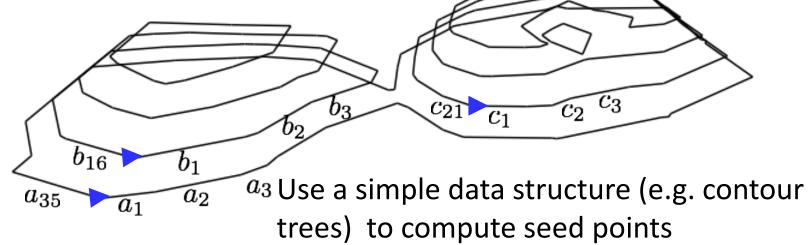
p the mean Denfity of the Earth. 757 of the fame relative altitude: by fo doing, I obtained a XXXIII. An Account of the Calculations made from the Survey and Meafures taken at Schehallien, in order to afcertain the mean Denfity of the Earth. By Charles Hutton, E/q. F. R. S.

> feveral of them paffing through it, I was thereby able to determine the altitude belonging to each fpace with much eafe and accuracy. In this estimation I could ge-

of

Computing Contour Map: Internal Memory Algorithm

Find a *seed* point on each contour and traverse the triangulation to trace each contour



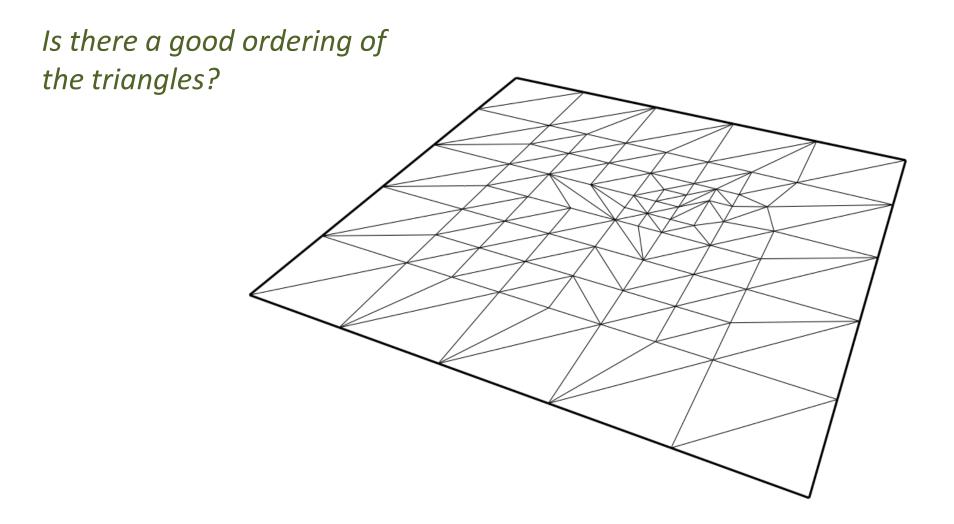
Query time: O(log N + T) T: #contour edges

Contour map: O(Nlog N +T) T: #contour map edges

For massive terrains

I/O efficiency is bad: O(N+T) instead of O((N+T)/B)

Storing a TIN on a disk so that it can be traversed with as few I/Os possible



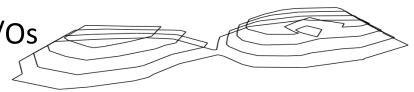
Our results

Ordering Theorem: A total ordering, called **C-ordering**, of triangles can be computed in O(Sort(N)) I/Os s.t. the subsequence of triangles intersecting a contour appears along the contour and contours in a level set are broken in nested order.

 $a_1a_2 - -b_1 - - -c_1c_2c_3 - - - -b_2b_3 - d_1d_2 - -b_4 - -a_3a_4a_5$

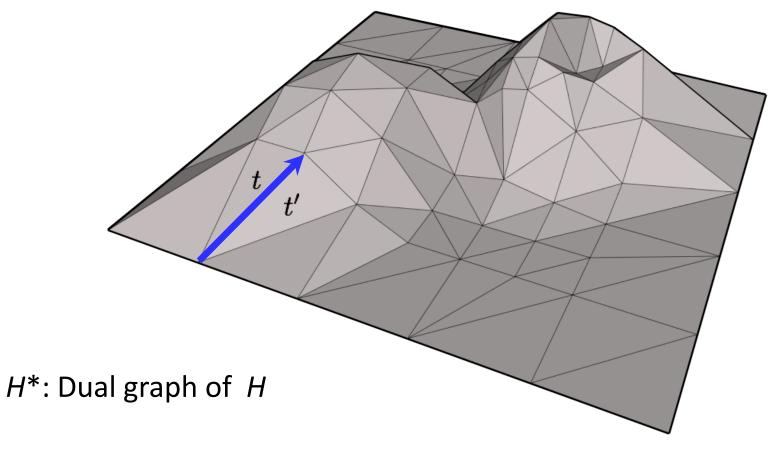
Individual contours can be retrieved in O(T/B)I/Os from this ordering

- Computing contour maps: O(Sort(N)+T/B) I/Os
- Answering contour queries
 - Preprocessing Time: O(Sort(N)) I/Os
 - Space: O(N/B) disk blocks
 - Query: O(log_BN+T/B)



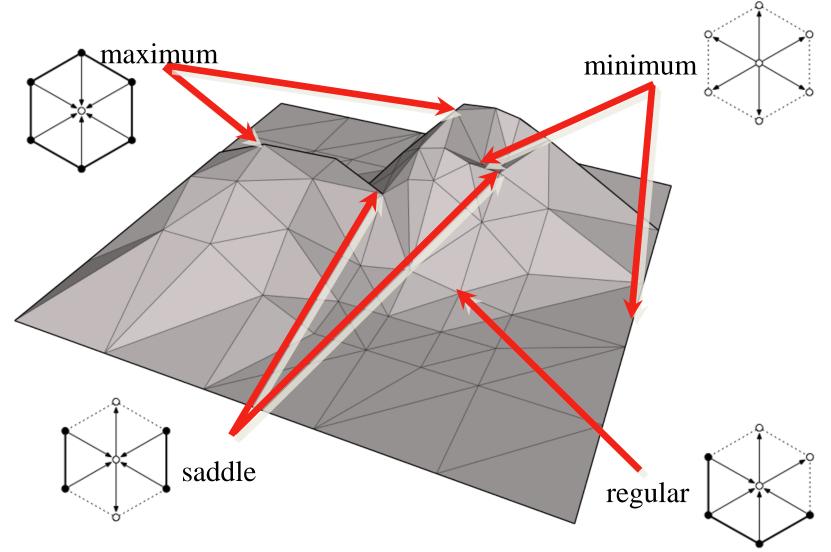
Height Graph

 $H = (V(\Sigma), \{u \to v : uv \in E(\Sigma), f(u) < f(v)\})$



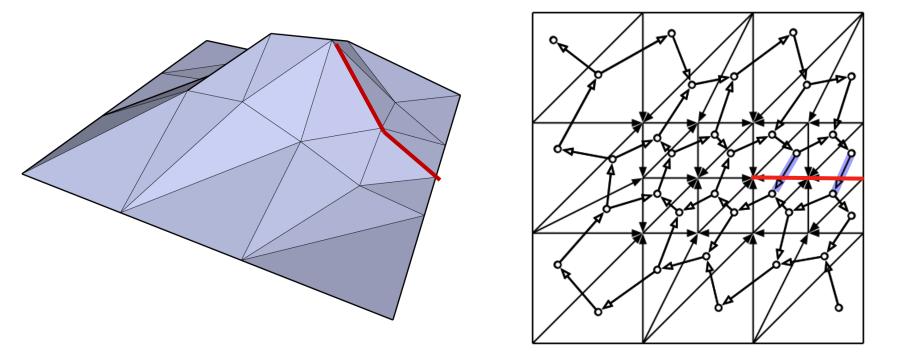
 $t \prec t'$ iff $t^* \to t'^*$ in H^* .

Critical Points



Simple Terrains

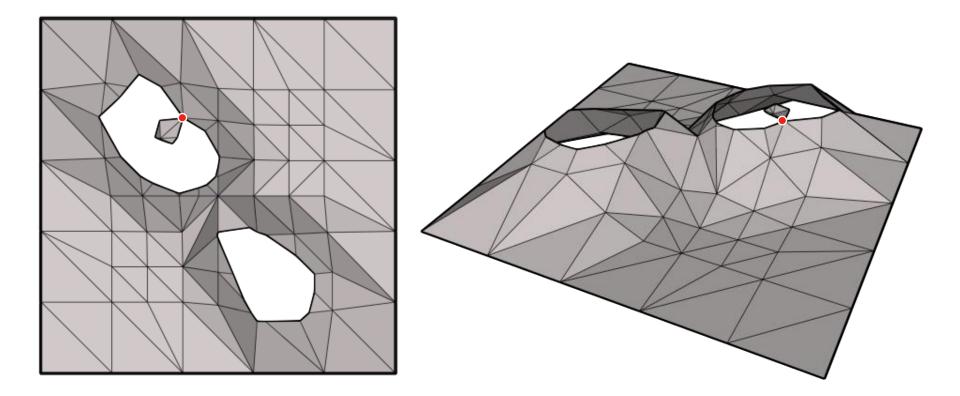
A simple terrain is one with no saddles; thus 1 max and 1 min (boundary). Take a min (bd) to max path P and delete its dual from H^* .



Once the dual graph becomes acyclic, the induced relation " \prec " becomes a partial order which can then be topologically sorted into a total order.

Positive & Negative Saddles

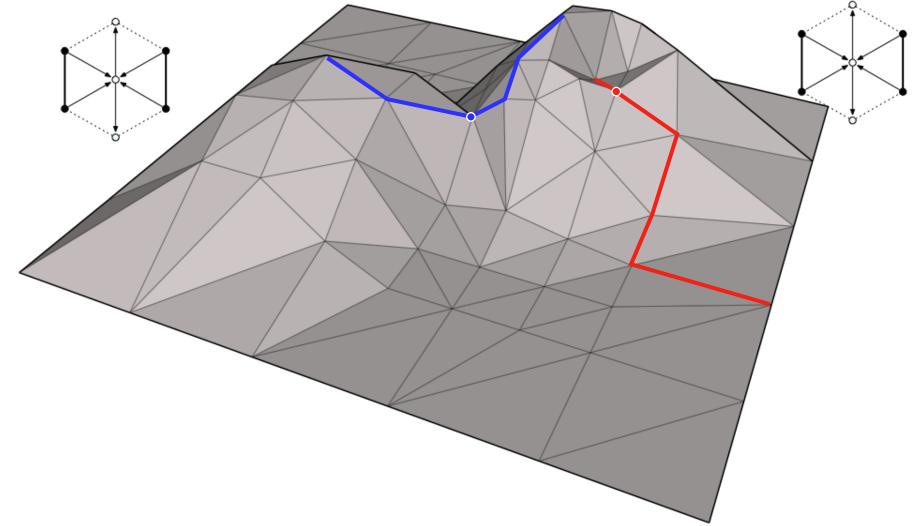
A saddle is negative if it joins two disjoint connected components of its sublevel-set and positive otherwise.



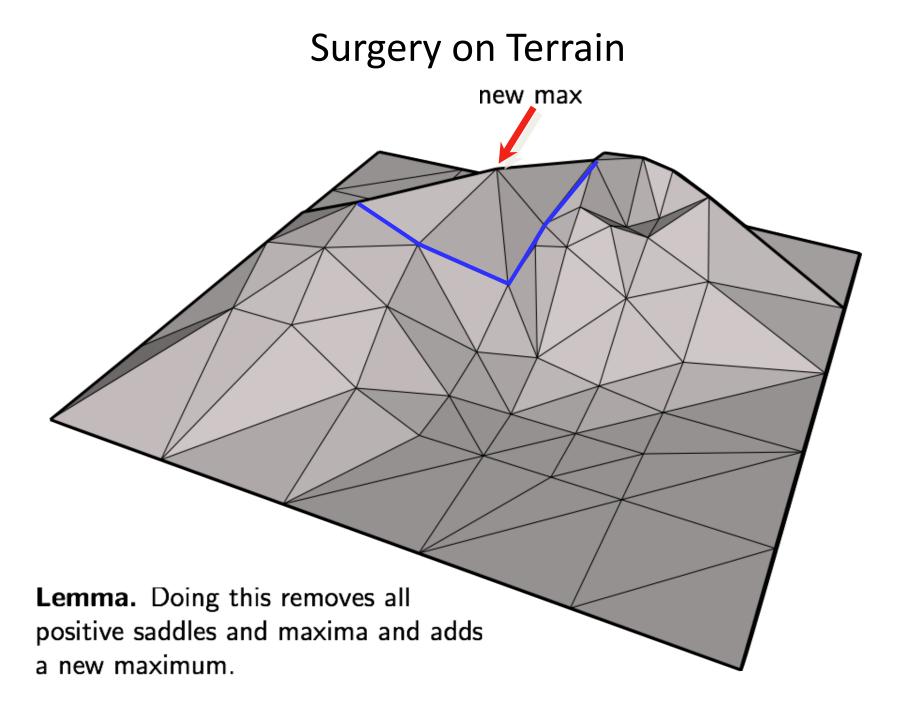
If we replace f with -f, the two types switch roles.

Cut Trees

Positive Cut-Tree: follow an ascending path in every connected component of the upper link of every positive saddle, joining paths when they collide.

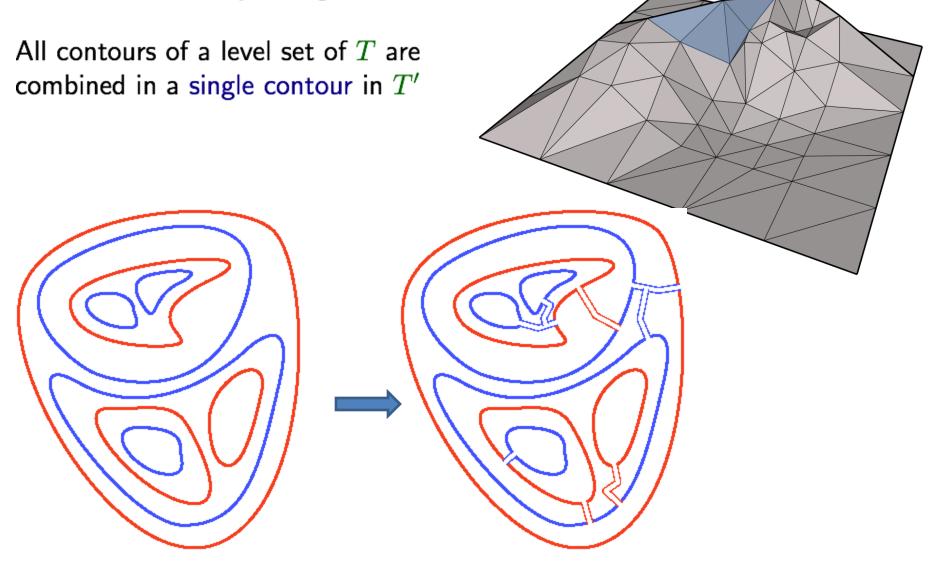


Lemma. The result is a tree (not just forest) that reaches every maximum.



Surgery & Contours

The simplified terrain T' has all the triangles of the original terrain T plus a number of auxiliary triangles.



Nesting of Contours

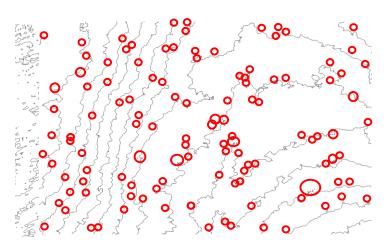
Theorem. In any contour of T', contours of T are broken (by segments from auxiliary triangles) in a nested (parenthesized) manner.

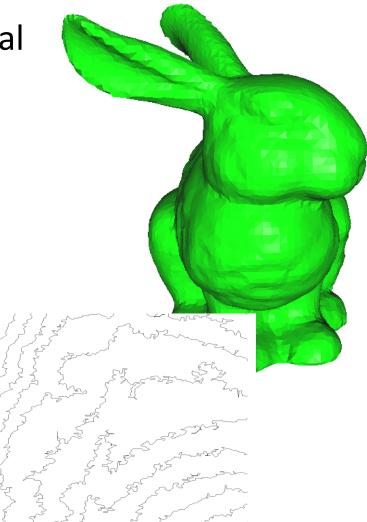
$$[a_1a_2 - b_1 - c_1c_2c_3 - b_2b_3 - d_1d_2 - b_4 - a_3a_4a_5]$$

This results a simple stack algorithm that separates tracks belonging to individual contours in O(T/B) I/Os.

Ongoing Work

- Compute C-ordering for general manifolds
- Maintain C-ordering for hierarchical representation of terrains
- Denoising contours





Collaborators









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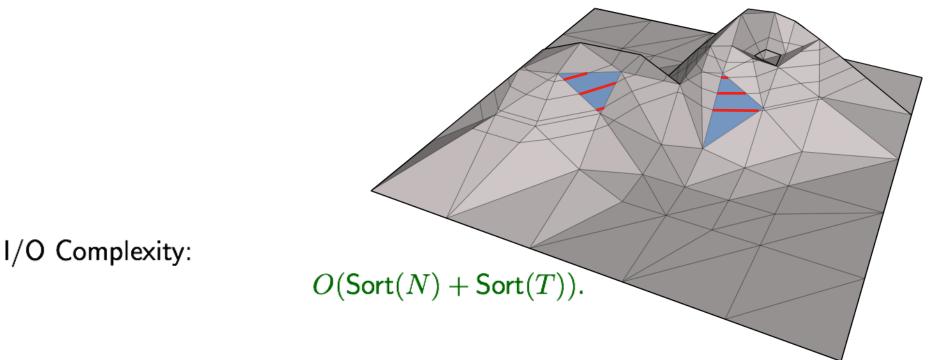
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I/O-Efficient Algorithms

Scan the triangles (in the order laid out on the disk) and generate all segments. Then sort the output.



Answering a contour query:

Preprocessing O(Nlog_BN), Space: O(N/B) blocks Query: O(log_BN+1/B)

