



THE UNIVERSITY OF  
CHICAGO

Department of Statistics

## DISSERTATION PRESENTATION AND DEFENSE

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Contact Processes on Random Regular Graphs

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Eckhart 110, 5734 S. University Avenue

### ABSTRACT

In this dissertation we mainly study the contact process on random regular graphs with growing sizes. Since the local geometry of a random regular graph resembles that of a regular tree  $\mathbb{T}^d$ , the appropriate analogue of the supercritical regime on  $\mathbb{T}^d$  is to choose the infection parameter  $\lambda > \lambda_1(\mathbb{T}^d)$ , the lower critical value on  $\mathbb{T}^d$ . We show in this case, for two typical vertices  $u, v$  on a typical graph  $G$ , a contact process initiated from  $u$  will infect  $v$  before time  $(C - \epsilon) \log n$  with vanishing probability, while it will infect  $v$  at time  $(C + \epsilon) \log n$  with a fixed positive probability.

A closely related problem is to study the extinction time  $\tau_n$ , the first time a contact process started from the full occupancy state reaches  $\emptyset$  on a graph of size  $n$ . When  $\lambda > \lambda_1(\mathbb{T}^d)$ , we show that  $\tau_n$  grows exponentially with  $n$ . Then, we show that the normalized extinction time,  $\tau_n / \mathbb{E}_G \tau_n$ , converges in law to a unit exponential distribution. We also determine the density of the infections of the quasi-stationary state.