



The University of Chicago  
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## PhD Dissertation Proposal Presentation

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### Understanding the Local Behavior of Unevenly Spaced Isotropic Stationary Gaussian Processes

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#### **ABSTRACT**

Consider the problem of estimating the parameters  $C$  and  $\alpha$  of a stationary isotropic Gaussian process in  $\mathbb{R}$  or  $\mathbb{R}^2$  with a covariance function  $\sigma(t) = \sigma(0) - C||t||^\alpha + o(||t||^\alpha)$  as  $||t|| \rightarrow 0$  for  $0 < \alpha < 2$ . Estimating a variance function of a random process is important in getting an accurate prediction. Furthermore, when the process is self-similar,  $\alpha$  has a nice simple relation with a fractal index  $D$ . Fractal theory has been well developed as one of the methods of quantifying the roughness of a curve or a surface. However most of the research has been limited to grid data assuming that the observations are evenly distributed. Also a high correlation between  $\hat{C}$  and  $\hat{\alpha}$  have made joint estimation hard.

This talk is on the expansion of the theory to unevenly spaced data to jointly estimate variance parameters. Here we assume a fixed-domain asymptotics as in the previous papers. We extend a concept of increments and suggest a nonlinear regression of squared increments to their expected values.